

	Project:	Project
	Location:	Location
	Client:	Client
	Job No.:	1
	Subject:	Beam
ANALYSIS & DESIGN OF RC BEAM AS PER ACI 318		

INPUT DATA

MATERIAL PROPERTIES

f'_c	=	41	Mpa	CONCRETE STRENGTH
f_y	=	414	Mpa	REBAR YIELD STRESS
f_{ys}	=	414	Mpa	LINKS YIELD STRESS
E_s	=	200,000	Mpa	Steel Modulus of Elasticity
E_c	=	30,095	Mpa	$E_c = 4700 * \text{SQRT}(f'_c)$

DIMENSIONS

L	=	3.15	m	BEAM LENGTH
B	=	200	mm	BEAM WIDTH
H	=	400	mm	BEAM HEIGHT
C_t	=	40	mm	COVER TO TOP REINFORCEMENT
C_c	=	40	mm	COVER TO BOTTOM REINFORCEMENT
C_s	=	40	mm	COVER TO SIDE BARS

STEEL REINFORCEMENT

LEFT SUPPORT

TOP REINFORCEMENT

layer 1		layer 2		layer space
no.	mm	no.	mm	
3	Ø 25	6	Ø 20	25

BOTTOM REINFORCEMENT

layer 1		layer 2		layer space
no.	mm	no.	mm	
2	Ø 25	2	Ø 25	25

HOOPS

no.	spacing	no.	spacing
1	50	11	85

MIDSPAN

TOP REINFORCEMENT

layer 1		layer 2	
no.	mm	no.	mm
2	Ø 25	3	Ø 25

BOTTOM REINFORCEMENT

layer 1		layer 2	
no.	mm	no.	mm
3	Ø 25	2	Ø 16

STIRRUPS

legs	mm	spacing
2	Ø 10	350

APPLIED FORCES

LEFT SUPPORT

M_u	=	200.00	kN-m
M_a	=	50.00	kN-m
V_u	=	150.00	kN
T_u	=		kN-m
P_u	=		kN-m

MIDSPAN

M_u	=	150.00	kN-m
M_a	=	25.00	kN-m

OUTPUT RESULTS

FLEXURAL CAPACITY CHECKS

LEFT SUPPORT

β_1	=	0.757142857	
c	=	153.14	mm
a	=	115.95	mm
ρ	=	0.0523	
$\rho_{(min)}$	=	0.0039	
ρ_b	=	0.0377	
ρ_g	=	0.0665	
$\rho_{(max)}$	=	N.A.	
$A_s_{(min)}$	=	248.11	mm ²
$A_s_{(max)}$	=	2,546.2	mm ²
ϵ_c	=	0.003	
ϵ'_s	=	0.0015	
f'_s	=	296.35	Mpa
A_s2	=	1405.52	mm ²
A_s1	=	1952.06	mm ²
ϵ_t	=	0.0033	
ϕ	=	0.75	
ϕ_{Mn}	=	266.82	kN-m

$\beta_1 = \text{max. of: } 0.85 - (0.05 * (f'_c - 28) / 7) \text{ and } 0.65$
 Solve for "c" in: $A_s * f_y = 0.85 * f'_c * \beta_1 * c * b + A'_s * (c - d')$
 $a = \beta_1 * c$
 $\rho = A_s / (b * d)$
 $\rho_{(min)} \geq 0.25 * \text{SQRT}(f'_c) / f_y \geq 1.4 / f_y$
 $\rho_b = 0.85 * \beta_1 * f'_c / f_y * (600 / (600 + f_y))$
 $\rho_g = (A_s + A'_s) / (b * h)$
 $\rho_{(max)} = A_s_{(max)} / (b * d)$
 $A_s_{(min)} = \rho_{(min)} * b * d$
 $A_s_{(max)} = (0.85 * f'_c * \beta_1 * c * b + A'_s * (c - d') / c * \epsilon_c * E_s) / f_y$ for $\epsilon_c = 0.003$ (assumed concrete strain)
 $\epsilon'_s = \epsilon_c * (c - d') / c < f_y / E_s, f'_s < d$
 $f'_s = \epsilon'_s * E_s$
 $A_s2 = A'_s * f'_s / f_y$ for $f'_s > 0$
 $A_s1 = A_s - A_s2$ for $f'_s > 0$
 $\epsilon_t = \epsilon_c * (d - c) / c = (f_y / E_s + \epsilon_c) / (\rho / \rho_b) - \epsilon_c$
 $\phi = 0.65 + 0.25 * (\epsilon_t - f_y / E_s) / (0.005 - f_y / E_s) \leq 0.90$
 $> M_u = 200 \text{ kN-m, O.K.}$

MIDSPAN

β_1	=	0.757142857	
c	=	99.47	mm
a	=	75.31	mm
ρ	=	0.0278	
$\rho_{(min)}$	=	0.0039	
ρ_b	=	0.0377	
ρ_g	=	0.0541	
$\rho_{(max)}$	=	N.A.	
$A_s_{(min)}$	=	261.18	mm ²
$A_s_{(max)}$	=	2,854.5	mm ²
ϵ_c	=	0.003	
ϵ'_s	=	0.0005	
f'_s	=	102.36	Mpa
A_s2	=	606.81	mm ²
A_s1	=	1267.93	mm ²

$\beta_1 = \text{max. of: } 0.85 - (0.05 * (f'_c - 28) / 7) \text{ and } 0.65$
 Solve for "c" in: $A_s * f_y = 0.85 * f'_c * \beta_1 * c * b + A'_s * (c - d')$
 $a = \beta_1 * c$
 $\rho = A_s / (b * d)$
 $\rho_{(min)} \geq 0.25 * \text{SQRT}(f'_c) / f_y \geq 1.4 / f_y$
 $\rho_b = 0.85 * \beta_1 * f'_c / f_y * (600 / (600 + f_y))$
 $\rho_g = (A_s + A'_s) / (b * h)$
 $\rho_{(max)} = A_s_{(max)} / (b * d)$
 $A_s_{(min)} = \rho_{(min)} * b * d$
 $A_s_{(max)} = (0.85 * f'_c * \beta_1 * c * b + A'_s * (c - d') / c * \epsilon_c * E_s) / f_y$ for $\epsilon_c = 0.003$ (assumed concrete strain)
 $\epsilon'_s = \epsilon_c * (c - d') / c < f_y / E_s, f'_s < d$
 $f'_s = \epsilon'_s * E_s$
 $A_s2 = A'_s * f'_s / f_y$ for $f'_s > 0$
 $A_s1 = A_s - A_s2$ for $f'_s > 0$

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ANALYSIS & DESIGN OF RC BEAM AS PER ACI 318

<p> ϵ_t = 0.0072 ϕ = 0.90 ϕM_n = 199.48 kN-m RIGHT SUPPORT β_1 = 0.757142857 c = 114.52 mm a = 86.71 mm ρ = 0.0387 ρ (min) = 0.0039 ρ_b = 0.0377 ρ_g = 0.0614 ρ (max) = N.A. A_s (min) = 245.53 mm² A_s (max) = 2,610.0 mm² ϵ_c = 0.003 ϵ'_s = 0.0008 f'_s = 167.76 Mpa A_s2 = 994.57 mm² A_s1 = 1459.80 mm² ϵ_t = 0.0053 ϕ = 0.90 ϕM_n = 236.20 kN-m </p>	<p> $\epsilon_t = \epsilon_c * (d-c) / c = (f_y / E_s + \epsilon_c) / (\rho / \rho_b) - \epsilon_c$ $\phi = 0.65 + 0.25 * (\epsilon_t - f_y / E_s) / (0.005 - f_y / E_s) \leq 0.90$ $> \mu = 150$ kN-m, O.K. $\beta_1 = \max. \text{ of: } 0.85 - (0.05 * (f'_c - 28) / 7) \text{ and } 0.65$ Solve for "c" in: $A_s * f_y = 0.85 * f'_c * \beta_1 * c * b + A'_s * (c - d')$ $a = \beta_1 * c$ $\rho = A_s / (b * d)$ ρ (min) $\geq 0.25 * \text{SQRT}(f'_c) / f_y \geq 1.4 / f_y$ $\rho_b = 0.85 * \beta_1 * f'_c / f_y * (600 / (600 + f_y))$ $\rho_g = (A_s + A'_s) / (b * h)$ ρ (max) = A_s (max) / (b * d) A_s (min) = ρ (min) * b * d A_s (max) = $(0.85 * f'_c * \beta_1 * c * b + A'_s * (c - d') / c * \epsilon_c * E_s) / f_y$ for $\epsilon_c = 0.003$ (assumed concrete strain) $\epsilon'_s = \epsilon_c * (c - d') / c < f_y / E_s, f'_s$ d $f'_s = \epsilon'_s * E_s$ $A_s2 = A'_s * f'_s / f_y$ for $f'_s > 0$ $A_s1 = A_s - A_s2$ for $f'_s > 0$ $\epsilon_t = \epsilon_c * (d - c) / c = (f_y / E_s + \epsilon_c) / (\rho / \rho_b) - \epsilon_c$ $\phi = 0.65 + 0.25 * (\epsilon_t - f_y / E_s) / (0.005 - f_y / E_s) \leq 0.90$ $> \mu = 159$ kN-m, O.K. </p>
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SHEAR CAPACITY CHECKS

<p>@ 2H for Seismic Provision for transverse Reinforcements per Sec.21.5.3.2 S (max) = smallest of ==></p>		<p> S (max) = $d/4$ S (max) = $8d_b$ (smallest longitudinal bar) S (max) = $24d_b$ (diameter of hoop bar) S (max) = 300mm </p>
<p> S (max) = 80.21 mm.o.c. < 85mm, N.G. </p>		

For Shear Reinforcements

<p> ϕV_c = 52.39 kN ϕV_s = 44.71 kN ϕV_n = 97.09 kN ϕV_s (max) = 203.38 kN A_v (prov) = 157.08 mm² A_v (req'd) = 388.97 mm² A_v (min) = 67.12 mm² S (max) = 160.42 mm </p>	<p> $\phi V_c = 0.17 * \lambda * \text{SQRT}(f'_c) * b * d$ $\phi V_s = \phi * f_y * d * A_v (\text{stirrup}) / s \geq 0$ $< V_u = 150$ kN, not O.K. $> V_u - (\phi) V_c = 97.61$ kN, O.K. $> A_v$ (prov) = 157.08, N.G. $\leq A_v$ (prov) = 157.08 mm², O.K. $< s = 350$ mm, N.G. </p>
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For Torsion Reinforcements

<p> T_c = 2.13 kN-m $T_{u\max}$ = N.A. kN-m A_t (prov) = N.A. mm² A_t (req'd) = N.A. mm² A_t (min) = N.A. mm² A_l (req'd) = N.A. mm² A_l (min) = N.A. mm² A_l (prov) = 1,963.50 mm² </p>	<p> < 0.00 kN-m, torsion need not to be considered! $(A_v + t (\text{used}) - A_v (\text{req'd})) / 2$ add'l web bars are not required! </p>
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Total (Av+t)	=	N.A.	mm ²
Total (Av+t) _{min}	=	N.A.	mm ²

CRACK CONTROL

<p> E_s = 200,000 MPa E_c = 30,095 MPa n = 6.65 </p>	<p> Steel Modulus of Elasticity $E_c = 4700 * \text{SQRT}(f'_c)$ $n = E_s / E_c$ </p>
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LEFT SUPPORT

<p> f_s = 1,834.20 MPa f_s (used) = 276.00 MPa s (max) = 260.51 mm s (min) = 25.00 mm s (act) = 33.33 mm </p>	<p> $f_s = M_a / (A_s * d * (1 - (\text{SQRT}(2 * A_s / (b * d) * n + (A_s / (b * d) * n)^2) - f_s (\text{used}) = \text{minimum of: } f_s \text{ and } 2/3 * f_y$ $s (\text{max}) = \text{minimum of: } 380 * 280 / f_s (\text{used}) - 2.5 * C_c \text{ and } 3$ $s (\text{min}) \leq s (\text{act}) \leq s (\text{max}), \text{ O.K.!$ </p>
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MIDSPAN

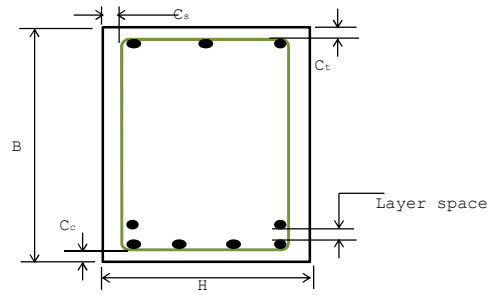
<p> f_s = 655.14 MPa f_s (used) = 276.00 MPa s (max) = 260.51 mm s (min) = 25.00 mm s (act) = 33.33 mm </p>	<p> $f_s = M_a / (A_s * d * (1 - (\text{SQRT}(2 * A_s / (b * d) * n + (A_s / (b * d) * n)^2) - f_s (\text{used}) = \text{minimum of: } f_s \text{ and } 2/3 * f_y$ $s (\text{max}) = \text{minimum of: } 380 * 280 / f_s (\text{used}) - 2.5 * C_c \text{ and } 3$ $s (\text{min}) \leq s (\text{act}) \leq s (\text{max}), \text{ O.K.!$ </p>
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RIGHT SUPPORT

<p> f_s = 1,016.80 MPa f_s (used) = 276.00 MPa s (max) = 260.51 mm s (min) = 25.00 mm s (act) = 50.00 mm </p>	<p> $f_s = M_a / (A_s * d * (1 - (\text{SQRT}(2 * A_s / (b * d) * n + (A_s / (b * d) * n)^2) - f_s (\text{used}) = \text{minimum of: } f_s \text{ and } 2/3 * f_y$ $s (\text{max}) = \text{minimum of: } 380 * 280 / f_s (\text{used}) - 2.5 * C_c \text{ and } 3$ $s (\text{min}) \leq s (\text{act}) \leq s (\text{max}), \text{ O.K.!$ </p>
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Calc. by:	RCF	Checked by:	RCF
Date:	26-Mar-11	Revision:	-

-08



RIGHT SUPPORT

TOP REINFORCEMENT

layer space	layer 1		layer 2		layer space
25	no.	mm	no.	mm	25
	2	Ø 25	3	Ø 25	

BOTTOM REINFORCEMENT

layer space	layer 1		layer 2		layer space
25	no.	mm	no.	mm	25
	2	Ø 25	3	Ø 25	

ADDITIONAL LONGITUDINAL BARS

no.	mm
4	Ø 10

RIGHT SUPPORT

Mu	=	159.00	kN-m
Ma	=	43.00	kN-m
Vu	=	76.00	kN
Tu	=		kN-m
Pu	=		kN-m

/c*ec*Es

or $c = \epsilon c \cdot d / (\epsilon c + 0.005)$

does not yield

Transition section

/c*ec*Es

or $c = \epsilon c \cdot d / (\epsilon c + 0.005)$

does not yield

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>= 0.005, Tension-controlled

/c*ec*Es

or $c = \epsilon c * d / (\epsilon c + 0.005)$

does not yield

>= 0.005, Tension-controlled

$A_s / (b * d) * n / 3$

$00 * 280 / f_s$ (used)

$A_s / (b * d) * n / 3$

$00 * 280 / f_s$ (used)

$A_s / (b * d) * n / 3$

$00 * 280 / f_s$ (used)